

SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR
(AUTONOMOUS)

B.Tech II Year II Semester Regular & Supplementary Examinations August-2023
DISCRETE MATHEMATICS

(Common to CSE, CSIT, CIC,CCC, CAD & CSM)

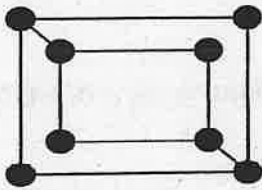
Time: 3 Hours

Max. Marks: 60

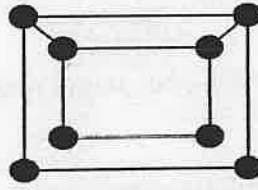
(Answer all Five Units 5 x 12 = 60 Marks)

UNIT-I

- 1 a Give an example of a graph that has neither an Eulerian circuit nor a Hamiltonian cycle. CO1 L1 6M
b Show that the given figures G1 and G2 are not isomorphic. CO1 L2 6M



G1



G2

OR

- 2 Explain Depth- First-Search, Breadth-First-Search Algorithm. CO1 L2 12M

UNIT-II

- 3 a Explain principle disjunctive normal form? Obtain the PDNF of $P \rightarrow ((P \rightarrow Q) \wedge \neg(\neg Q \vee \neg P))$ CO2 L5 6M
b Explain principle conjunctive normal form? Obtain the PCNF of $(\neg P \rightarrow R) \wedge (Q \leftrightarrow P)$ CO2 L5 6M

OR

- 4 a Show that $\sim P$ is a valid conclusion from the premises $\sim(P \wedge \sim Q)$, $\sim Q \vee R$, $\sim R$ CO2 L2 6M
b Show that $(\exists x) M(x)$ follows logically from the premises $(\forall x)(H(x) \rightarrow M(x))$ and $(\exists x)H(x)$. CO2 L2 6M

UNIT-III

- 5 Let A be a given finite set and P(A) its power set. let \subseteq be the inclusion relation on the elements of P(A). Draw the Hasse diagram of $(P(A), \subseteq)$ for

- i) $A = \{ a \}$
ii) $A = \{ a, b \}$
iii) $A = \{ a, b, c \}$
iv) $A = \{ a, b, c, d \}$.

OR

- 6 a On the set Q of all rational number operation * is defined by $a * b = a + b - ab$, Show that this operation Q forms a commutative monoid. CO4 L2 6M
b Show that the set $\{1, 2, 3, 4, 5\}$ is not a group under addition and multiplication modulo 6. CO4 L2 6M

UNIT-IV

- 7 a Enumerate the number of non- negative integral solutions to the inequality $x_1 + x_2 + x_3 + x_4 + x_5 \leq 19$. CO5 L3 6M
- b How many integral solutions are there to $x_1 + x_2 + x_3 + x_4 + x_5 = 20$ where each (i) $x_i \geq 2$ (ii) $x_i > 2$ CO5 L3 6M

OR

- 8 a Applying pigeon hole principle show that of any 14 integers are selected from the set $S = \{1, 2, 3, \dots, 25\}$ there are at least two whose sum is 26. Also write a statement that generalizes this result. CO5 L2 6M
- b Show that if 8 people are in a room, at least two of them have birthdays that occur on the same day of the week. CO5 L2 6M

UNIT-V

- 9 a Solve $a_n = a_{n-1} + 2a_{n-2}, n \geq 2$ with the initial conditions $a_0 = 0, a_1 = 1$. CO6 L3 6M
- b Solve $a_{n+2} - 5a_{n+1} + 6a_n = 2$ with the initial conditions $a_0 = 1, a_1 = -1$ CO6 L3 6M

OR

- 10 a Solve $a_n - 5a_{n-1} + 6a_{n-2} = 2^n, n \geq 2$ with the initial conditions $a_0 = 1, a_1 = 1$. Using generating functions. CO6 L3 6M
- b Solve $a_n - 4a_{n-1} + 4a_{n-2} = (n+1)^2$ given $a_0 = 0, a_1 = 1$ CO6 L3 6M

*** END ***